

$$\mathbf{F}(x, y) = e^{-y} \mathbf{i} - xe^{-y} \mathbf{j}, W = \int_C \mathbf{F} \cdot d\mathbf{r}.$$

Since $\frac{\partial}{\partial y}(e^{-y}) = -e^{-y} = \frac{\partial}{\partial x}(-xe^{-y})$, there exists a function f such that $\nabla f = \mathbf{F}$. In fact, $f_x = e^{-y} \Rightarrow f(x, y) = xe^{-y} + g(y) \Rightarrow f_y = -xe^{-y} + g'(y) \Rightarrow g'(y) = 0$, so we can take $f(x, y) = xe^{-y}$ as a potential function for \mathbf{F} .

$$\text{Thus } W = \int_C \mathbf{F} \cdot d\mathbf{r} = f(4, 0) - f(0, 2) = 4 - 0 = 4.$$