

Let  $u = 7 \arccos x$ ,  $dv = dx \Rightarrow du = -\frac{7dx}{\sqrt{1-x^2}}$ ,  $v = x$ .

Then  $I = \int_0^{1/2} 7 \arccos x dx = [7x \arccos x]_0^{1/2} + 7 \int_0^{1/2} \frac{x dx}{\sqrt{1-x^2}}$   
 $= \frac{7}{2} \cdot \frac{\pi}{3} + 7 \int_1^{3/4} t^{-1/2} [-\frac{1}{2} dt]$ , where  $t = 1 - x^2 \Rightarrow dt = -2x dx$ .

Thus,  $I = \frac{7\pi}{6} + \frac{7}{2} \int_{3/4}^1 t^{-1/2} dt = \frac{7\pi}{6} + 7 [\sqrt{t}]_{3/4}^1 = \frac{7\pi}{6} + 7 - 7\frac{\sqrt{3}}{2}$   
 $= \frac{7}{6}(\pi + 6 - 3\sqrt{3})$ .