$$a_n = n^2 e^{-5n} = \frac{n^2}{e^{5n}}$$
. Since $\lim_{x \to \infty} \frac{x^2}{e^{5x}} \stackrel{\text{H}}{=} \lim_{x \to \infty} \frac{2x}{5e^{5x}} \stackrel{\text{H}}{=} \lim_{x \to \infty} \frac{2}{25e^{5x}} = 0$, it follows that $\lim_{n \to \infty} a_n = 0$. Converges