

$$\begin{aligned}\int_0^1 \int_0^v 8\sqrt{1-v^2} \, du \, dv &= \int_0^1 \left[8u \sqrt{1-v^2} \right]_{u=0}^{u=v} \, dv = \int_0^1 8v \sqrt{1-v^2} \, dv \\ &= -\frac{8}{3} (1-v^2)^{3/2} \Big|_0^1 = -\frac{8}{3} (0-1) = \frac{8}{3}\end{aligned}$$