

$$\lim_{t \rightarrow 0^+} \tan(t) = \tan(0) = 0, \quad \lim_{t \rightarrow 0^+} \cos(t) = \cos(0) = 1,$$

$$\lim_{t \rightarrow 0^+} t^3 \ln(t) = \lim_{t \rightarrow 0^+} \frac{\ln(t)}{1/t^3} = \lim_{t \rightarrow 0^+} \frac{1/t}{-3/t^4} = \lim_{t \rightarrow 0^+} -t^3/3 = 0 \quad [\text{by l'Hospital's Rule}].$$

$$\begin{aligned} \text{Thus } \lim_{t \rightarrow 0^+} \langle \tan(t), \cos(t), t^3 \ln(t) \rangle &= \left\langle \lim_{t \rightarrow 0^+} \tan(t), \lim_{t \rightarrow 0^+} \cos(t), \lim_{t \rightarrow 0^+} t^3 \ln(t) \right\rangle \\ &= \langle 0, 1, 0 \rangle. \end{aligned}$$