$\frac{2}{7} - \frac{2}{8} + \frac{2}{9} - \frac{2}{10} + \frac{2}{11} - \dots = \sum_{n=1}^{\infty} (-1)^{n-1} \frac{2}{n+6}.$  Now  $b_n = \frac{2}{n+6} > 0$ ,  $\{b_n\}$  is decreasing, and  $\lim_{n \to \infty} b_n = 0$ , so the series converges by the Alternating Series Test.