

$f(x, y) = 15x^3y/(2x^4 + y^4)$. On the x -axis, $f(x, 0) = 0$ for $x \neq 0$, so $f(x, y) \rightarrow 0$ as $(x, y) \rightarrow (0, 0)$ along the x -axis. Approaching $(0, 0)$ along the line $y = x$ gives $f(x, x) = 15x^4/(3x^4) = 5$ for $x \neq 0$, so along this line $f(x, y) \rightarrow 5$ as $(x, y) \rightarrow (0, 0)$. Thus the limit does not exist.