

Solving the equation for z gives $z^2 = 1 - 2x^2 - 3y^2 \Rightarrow$
 $z = -\sqrt{1 - 2x^2 - 3y^2}$ (since we want the lower half of the ellipsoid). If we
let u and v be the parameters, parametric equations are $x = u$, $y = v$,
 $z = -\sqrt{1 - 2u^2 - 3v^2}$.

Alternate solution: The equation can be rewritten as

$$\frac{x^2}{(1/\sqrt{2})^2} + \frac{y^2}{(1/\sqrt{3})^2} + z^2 = 1 , \text{ and if we let } x = \frac{1}{\sqrt{2}} u \cos v \text{ and}$$

$$y = \frac{1}{\sqrt{3}} u \sin v , \text{ then } z = -\sqrt{1 - 2x^2 - 3y^2} = -\sqrt{1 - u^2 \cos^2 v - u^2 \sin^2 v}$$

$$= -\sqrt{1 - u^2} , \text{ where } 0 \leq u \leq 1 \text{ and } 0 \leq v \leq 2\pi .$$