$\sqrt{8x+y}$ is defined only when $8x+y\geq 0$, or $y\geq -8x$. So the domain of f is $\{(x,y)\mid y\geq -8x\}$.

