

$$\begin{aligned} L &= \int_a^b \sqrt{r^2 + (dr/d\theta)^2} d\theta = \int_0^\pi \sqrt{(e^{2\theta})^2 + (2e^{2\theta})^2} d\theta \\ &= \int_0^\pi \sqrt{e^{4\theta} + 4e^{4\theta}} d\theta = \int_0^\pi \sqrt{5e^{4\theta}} d\theta \\ &= \sqrt{5} \int_0^\pi e^{2\theta} d\theta = \frac{\sqrt{5}}{2} [e^{2\theta}]_0^\pi = \frac{\sqrt{5}}{2} (e^{2\pi} - 1) \end{aligned}$$