

$\mathbf{F}(x, y, z) = xy \mathbf{i} + yz \mathbf{j} + zx \mathbf{k}$, $z = g(x, y) = 8 - x^2 - y^2$, and D is the square $[0, 1] \times [0, 1]$, so

$$\begin{aligned} \iint_S \mathbf{F} \cdot d\mathbf{S} &= \iint_D [-xy(-2x) - yz(-2y) + zx] dA \\ &= \int_0^1 \int_0^1 [2x^2y + 2y^2(8 - x^2 - y^2) + x(8 - x^2 - y^2)] dy dx \\ &= \int_0^1 \left(\frac{1}{3}x^2 + \frac{23}{3}x - x^3 + \frac{74}{15} \right) dx = \frac{1553}{180} \end{aligned}$$