

$$\begin{aligned}
\iint_D 7xy^2 \, dA &= \int_{-2}^2 \int_0^{\sqrt{4-y^2}} 7xy^2 \, dx \, dy = \int_{-2}^2 7y^2 \left[ \frac{1}{2}x^2 \right]_{x=0}^{x=\sqrt{4-y^2}} dy \\
&= \frac{7}{2} \int_{-2}^2 y^2(4-y^2) \, dy = \frac{7}{2} \int_{-2}^2 (4y^2 - y^4) \, dy \\
&= \frac{7}{2} \left[ \frac{4}{3}y^3 - \frac{1}{5}y^5 \right]_{-2}^2 = \frac{7}{2} \left( \frac{32}{3} - \frac{32}{5} + \frac{32}{3} - \frac{32}{5} \right) = \frac{448}{15}
\end{aligned}$$

