

The region of integration is given in spherical coordinates by

$$E = \{(\rho, \theta, \phi) \mid 2 \leq \rho \leq 4, 0 \leq \theta \leq \pi/2, \pi/2 \leq \phi \leq \pi\}.$$

This represents the solid region between the spheres $\rho = 2$ and $\rho = 4$ in the fifth octant.

$$\begin{aligned} \int_0^{\pi/2} \int_{\pi/2}^{\pi} \int_2^4 \rho^2 \sin(\phi) d\rho d\phi d\theta &= \int_0^{\pi/2} d\theta \int_{\pi/2}^{\pi} \sin(\phi) d\phi \int_2^4 \rho^2 d\rho \\ &= [\theta]_0^{\pi/2} [-\cos(\phi)]_{\pi/2}^{\pi} \left[\frac{1}{3}\rho^3\right]_2^4 \\ &= (\pi/2)(1)(56/3) = (28/3)\pi \end{aligned}$$

