

$\mathbf{F}(x, y, z) = xze^y \mathbf{i} - xze^y \mathbf{j} + z \mathbf{k}$, $z = g(x, y) = 5 - x - y$, and $D = \{(x, y) \mid 0 \leq x \leq 5, 0 \leq y \leq 5 - x\}$. Since S has downward orientation, we have

$$\begin{aligned} \iint_S \mathbf{F} \cdot d\mathbf{S} &= - \iint_D [-xze^y(-1) - (-xze^y)(-1) + z] dA \\ &= - \int_0^5 \int_0^{5-x} (5 - x - y) dy dx \\ &= - \int_0^5 \left(\frac{1}{2}x^2 - 5x + \frac{25}{2} \right) dx = -\frac{125}{6} \end{aligned}$$