

$\operatorname{div}\mathbf{F} = 3y^2 + 0 + 3z^2$, so using cylindrical coordinates
with $y = r \cos \theta$, $z = r \sin \theta$, $x = x$ we have

$$\begin{aligned}\iint_S \mathbf{F} \cdot d\mathbf{S} &= \iiint_E (3y^2 + 3z^2) dV \\ &= \int_0^{2\pi} \int_0^3 \int_{-3}^3 (3r^2 \cos^2 \theta + 3r^2 \sin^2 \theta) r dx dr d\theta \\ &= 3 \int_0^{2\pi} d\theta \int_0^3 r^3 dr \int_{-3}^3 dx = 3(2\pi) \left(\frac{81}{4}\right) (6) = 729\pi\end{aligned}$$