

$$a_n = \frac{n^3}{3n^3 + 1} = \frac{n^3/n^3}{(3n^3 + 1)/n^3} = \frac{1}{3 + 1/n^3},$$

so  $a_n \rightarrow \frac{1}{3+0} = \frac{1}{3}$  as  $n \rightarrow \infty$ . Converges