

$$\mathbf{r}(t) = t \mathbf{i} + 7t \mathbf{j} + (5 + t^2) \mathbf{k} \Rightarrow \mathbf{r}'(t) = \mathbf{i} + 7\mathbf{j} + 2t \mathbf{k}, \quad \mathbf{r}''(t) = 2 \mathbf{k},$$

$$|\mathbf{r}'(t)| = \sqrt{1^2 + 7^2 + (2t)^2} = \sqrt{4t^2 + 50}, \quad \mathbf{r}'(t) \times \mathbf{r}''(t) = 14 \mathbf{i} - 2 \mathbf{j},$$

$$|\mathbf{r}'(t) \times \mathbf{r}''(t)| = \sqrt{2^2 + 14^2 + 0^2} = \sqrt{200} = 2\sqrt{50}.$$

$$\begin{aligned} \text{Then } \kappa(t) &= \frac{|\mathbf{r}'(t) \times \mathbf{r}''(t)|}{|\mathbf{r}'(t)|^3} = \frac{2\sqrt{50}}{(\sqrt{4t^2 + 50})^3} = \frac{2\sqrt{2}\sqrt{25}}{(\sqrt{2}\sqrt{2t^2 + 25})^3} \\ &= \frac{\sqrt{25}}{(2t^2 + 25)^{3/2}}. \end{aligned}$$