- (a) True; each of the first two lines has a direction vector parallel to the direction vector of the third line, so these vectors are each scalar multiples of the third direction vector. Then the first two direction vectors are also scalar multiples of each other, so these vectors, and hence the two lines, are parallel.
- (b) False; for example, the x and y -axes are both perpendicular to the z -axis, yet the x and y -axes are not parallel.
- (c) True; each of the first two planes has a normal vector parallel to the normal vector of the third plane, so these two normal vectors are parallel to each other and the planes are parallel.
- (d) False; for example, the xy and yz -planes are not parallel, yet they are both perpendicular to the xz -plane.
- (e) False; the x and y -axes are not parallel, yet they are both parallel to the plane z = 1.
- (f) True; if each line is perpendicular to a plane, then the lines' direction vectors are both parallel to a normal vector for the plane. Thus, the direction vectors are parallel to each other and the lines are parallel.
- (g) False; the planes y = 1 and z = 1 are not parallel, yet they are both parallel to the x -axis.
- (h) True; if each plane is perpendicular to a line, then any normal vector for each plane is parallel to a direction vector for the line. Thus, the normal vectors are parallel to each other and the planes are parallel.
- (i) True.
- (j) False; they can be skew.
- (k) True. Consider any normal vector for the plane and any direction vector for the line. If the normal vector is perpendicular to the direction vector, the line and plane are parallel. Otherwise, the vectors meet at an angle θ , $0^{\circ} \leq \theta < 90^{\circ}$, and the line will intersect the plane at an angle $90^{\circ} \theta$.