

$$r = 8 \sin \theta \quad \Rightarrow \quad x = r \cos \theta = 8 \sin \theta \cos \theta = \frac{8}{2} \sin 2\theta, \quad y = r \sin \theta = 8 \sin^2 \theta$$

\Rightarrow

$$\frac{dy}{dx} = \frac{dy/d\theta}{dx/d\theta} = \frac{8 \cdot 2 \sin \theta \cos \theta}{4 \cdot 2 \cos 2\theta} = \frac{\sin 2\theta}{\cos 2\theta} = \tan 2\theta$$

$$\text{When } \theta = \frac{\pi}{6}, \quad \frac{dy}{dx} = \tan\left(2 \cdot \frac{\pi}{6}\right) = \tan \frac{\pi}{3} = \sqrt{3}.$$