

$$y = 7 \cos x \Rightarrow dy/dx = -7 \sin x \Rightarrow 1 + (dy/dx)^2 = 1 + 49 \sin^2 x. \text{ So}$$

$$L = \int_0^{2\pi} \sqrt{1 + 49 \sin^2 x} \, dx.$$