

$$\begin{aligned}f(x, y, z) &= \cos(2x + 2y + 4z) \quad \Rightarrow \\f_x &= -\sin(2x + 2y + 4z)(2) = -2\sin(2x + 2y + 4z), \\f_{xy} &= -2\cos(2x + 2y + 4z)(2) = -4\cos(2x + 2y + 4z), \\f_{xyz} &= -4(-\sin(2x + 2y + 4z))(4) = 16\sin(2x + 2y + 4z) \quad \text{and} \\f_y &= -\sin(2x + 2y + 4z)(2) = -2\sin(2x + 2y + 4z), \\f_{yz} &= -2\cos(2x + 2y + 4z)(4) = -8\cos(2x + 2y + 4z), \\f_{yzz} &= -8(-\sin(2x + 2y + 4z))(4) = 32\sin(2x + 2y + 4z).\end{aligned}$$