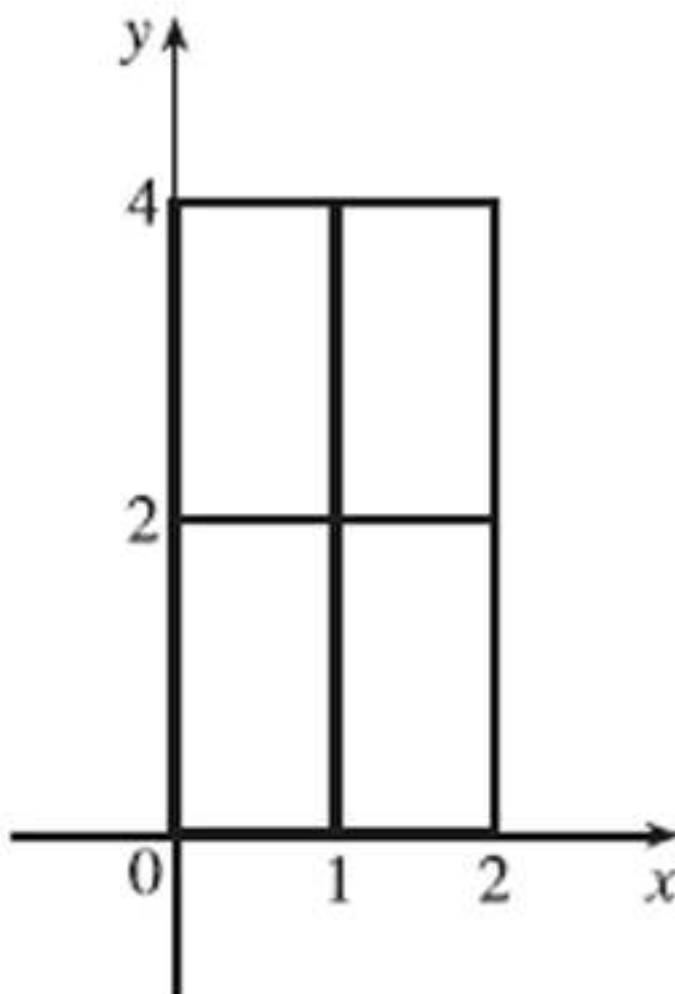


(a) The subrectangles are shown in the figure.

The surface is the graph of $f(x, y) = 9x + 5y^2$ and $\Delta A = 2$, so we estimate

$$\begin{aligned} V &= \iint_R (9x + 5y^2) dA \approx \sum_{i=1}^2 \sum_{j=1}^2 f(x_{ij}^*, y_{ij}^*) \Delta A \\ &= f(1, 0) \Delta A + f(1, 2) \Delta A + f(2, 0) \Delta A + f(2, 2) \Delta A \\ &= 9(2) + 29(2) + 18(2) + 38(2) = 188 \end{aligned}$$



$$\begin{aligned}
 \text{(b) } V &= \iint_R (9x + 5y^2) dA \approx \sum_{i=1}^2 \sum_{j=1}^2 f(\bar{x}_i, \bar{y}_j) \Delta A \\
 &= f\left(\frac{1}{2}, 1\right) \Delta A + f\left(\frac{1}{2}, 3\right) \Delta A + f\left(\frac{3}{2}, 1\right) \Delta A + f\left(\frac{3}{2}, 3\right) \Delta A \\
 &= \frac{19}{2}(2) + \frac{99}{2}(2) + \frac{37}{2}(2) + \frac{117}{2}(2) = 272
 \end{aligned}$$

