

$$\begin{aligned} \text{(a) } \operatorname{curl} \mathbf{F} &= \nabla \times \mathbf{F} = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ \partial/\partial x & \partial/\partial y & \partial/\partial z \\ 1 & x + yz & xy - 5\sqrt{z} \end{vmatrix} \\ &= (x - y)\mathbf{i} - (y - 0)\mathbf{j} + (1 - 0)\mathbf{k} \\ &= (x - y)\mathbf{i} - y\mathbf{j} + \mathbf{k} \end{aligned}$$

$$\text{(b) } \operatorname{div} \mathbf{F} = \nabla \cdot \mathbf{F} = \frac{\partial}{\partial x}(1) + \frac{\partial}{\partial y}(x + yz) + \frac{\partial}{\partial z}(xy - 5\sqrt{z}) = z - \frac{5}{2\sqrt{z}}$$