



Assume  $a = 2, b = 9$ .

The region of integration is given in cylindrical coordinates by  $E = \{(r, \theta, z) | 0 \leq \theta \leq \pi/2, 0 \leq r \leq 2, 0 \leq z \leq 9 - r^2\}$ .

This represents the solid region in the first octant enclosed by the circular cylinder  $r = 2$ , bounded above by  $z = 9 - r^2$ , a circular paraboloid, and bounded below by the  $xy$ -plane.

$$\begin{aligned}
 \int_0^{\pi/2} \int_0^2 \int_0^{9-r^2} r \, dz \, dr \, d\theta &= \int_0^{\pi/2} \int_0^2 [rz]_{z=0}^{z=9-r^2} \, dr \, d\theta \\
 &= \int_0^{\pi/2} \int_0^2 r(9 - r^2) \, dr \, d\theta = \int_0^{\pi/2} d\theta \int_0^2 (9r - r^3) \, dr \\
 &= [\theta]_0^{\pi/2} \left[ \frac{9}{2}r^2 - \frac{1}{4}r^4 \right]_0^2 = 7\pi
 \end{aligned}$$