

$\mathbf{F}(x, y) = \langle y^2 \cos x, x^2 + 2y \sin x \rangle$  and the region  $D$  enclosed by  $C$  is given by  $\{(x, y) \mid 0 \leq x \leq 4, 0 \leq y \leq 3x\}$ .  $C$  is traversed clockwise, so  $-C$  gives the positive orientation.

$$\begin{aligned} \int_C \mathbf{F} \cdot d\mathbf{r} &= - \int_{-C} (y^2 \cos x) dx + (x^2 + 2y \sin x) dy \\ &= - \iint_D \left[ \frac{\partial}{\partial x} (x^2 + 2y \sin x) - \frac{\partial}{\partial y} (y^2 \cos x) \right] dA \\ &= - \iint_D (2x + 2y \cos x - 2y \cos x) dA = - \int_0^4 \int_0^{3x} 2x dy dx \\ &= - \int_0^4 2x [y]_{y=0}^{y=3x} dx = - \int_0^4 6x^2 dx = - 2x^3 \Big|_0^4 = -128 \end{aligned}$$