The functions $\sin(xy)$ and $e^x - y^6$ are continuous everywhere, so $F(x, y) = \frac{\sin(xy)}{e^x - y^6}$ is continuous except where $e^x - y^6 = 0 \implies y^6 = e^x \implies y = \pm \sqrt[6]{e^x} = \pm e^{\frac{1}{6}x}$. Thus F is continuous on its domain $\{(x, y) \mid |y| \neq e^{x/6}\}$.