

- (a)  $x = 5 + \ln t, y = t^2 + 3; (5, 4)$ .  $\frac{dy}{dt} = 2t, \frac{dx}{dt} = \frac{1}{t}$ ,  
and  $\frac{dy}{dx} = \frac{dy/dt}{dx/dt} = \frac{2t}{1/t} = 2t^2$ . At  $(5, 4), x = 5 + \ln t = 5 \Rightarrow$   
 $\ln t = 0 \Rightarrow t = 1$  and  $\frac{dy}{dx} = 2$ , so an equation of the tangent is  
 $y - 4 = 2(x - 5)$ , or  $y = 2x - 6$ .
- (b)  $x = 5 + \ln t \Rightarrow x - 5 = \ln t \Rightarrow t = e^{x-5}$ , so  
 $y = t^2 + 3 = (e^{x-5})^2 + 3 = e^{2x-10} + 3$  and  $y' = e^{2x-10} \cdot 2$ .  
At  $(5, 4), y' = e^{2(5)-10} \cdot 2 = 2$ , so an equation of the tangent is  $y - 4 =$   
 $2(x - 5)$ , or  $y = 2x - 6$ .