

$$T = \frac{k}{\sqrt{x^2 + y^2 + z^2}} \text{ and } 120 = T(4, 4, 2) = \frac{k}{6} \text{ so } k = 720.$$

$$(a) \mathbf{u} = \frac{\langle 3, 1, 1 \rangle}{\sqrt{11}},$$

$$\begin{aligned} D_{\mathbf{u}}T(4, 4, 2) &= \nabla T(4, 4, 2) \cdot \mathbf{u} \\ &= \left[-720(x^2 + y^2 + z^2)^{-3/2} \langle x, y, z \rangle \right]_{(4,4,2)} \cdot \mathbf{u} \\ &= -\frac{10}{3} \langle 4, 4, 2 \rangle \cdot \frac{1}{\sqrt{11}} \langle 3, 1, 1 \rangle \\ &= -\frac{60}{\sqrt{11}} \end{aligned}$$

- (b) From (a), $\nabla T = -720(x^2 + y^2 + z^2)^{-3/2} \langle x, y, z \rangle$, and since $\langle x, y, z \rangle$ is the position vector of the point (x, y, z) , the vector $-\langle x, y, z \rangle$, and thus ∇T , always points toward the origin.