

The paraboloid $z = 5 - 5x^2 - 5y^2$ intersects the xy -plane in the circle $x^2 + y^2 = 1$, so

$$\begin{aligned} V &= \iint_{x^2+y^2 \leq 1} (5 - 5x^2 - 5y^2) \, dA = \iint_{x^2+y^2 \leq 1} [5 - 5(x^2 + y^2)] \, dA = \int_0^{2\pi} \int_0^1 (5 - 5r^2) \, r \, dr \, d\theta \\ &= \int_0^{2\pi} d\theta \int_0^1 (5r - 5r^3) \, dr = [\theta]_0^{2\pi} \left[\frac{5}{2}r^2 - \frac{5}{4}r^4 \right]_0^1 = (2\pi) \left(\frac{5}{2} - \frac{5}{4} \right) = \frac{5}{2}\pi \end{aligned}$$