

$a_n = \frac{x^n}{6^n n^4}$, so $\lim_{n \rightarrow \infty} \left| \frac{a_{n+1}}{a_n} \right| = \lim_{n \rightarrow \infty} \left| \frac{x^{n+1}}{6^{n+1} (n+1)^4} \cdot \frac{6^n n^4}{x^n} \right| = \lim_{n \rightarrow \infty} \frac{|x|}{6} \left(\frac{n}{n+1} \right)^4 = \frac{|x|}{6}$. By the Ratio Test, the series $\sum_{n=1}^{\infty} \frac{x^n}{6^n n^4}$ converges when $\frac{|x|}{6} < 1 \Leftrightarrow |x| < 6$, so $R = 6$. When $x = -6$, we get the series $\sum_{n=1}^{\infty} \frac{(-1)^n}{n^4}$, which converges by the Alternating Series Test. When $x = 6$, we get the convergent p -series $\sum_{n=1}^{\infty} \frac{1}{n^4}$ [$p = 4 > 1$]. Thus, $I = [-6, 6]$.