

By Green's Theorem,

$$W = \int_C \mathbf{F} \cdot d\mathbf{r} = \int_C 8x \, dx + (x^3 + 3xy^2) \, dy = \iint_D (3x^2 + 3y^2 - 0) \, dA,$$

where D is the semicircular region bounded by C . Converting to polar coordinates, we have

$$W = 3 \int_0^1 \int_0^\pi r^2 \cdot r \, d\theta \, dr = 3\pi \left[\frac{1}{4} r^4 \right]_0^1 = \frac{3}{4}\pi.$$