

$dA = \frac{\partial A}{\partial x} dx + \frac{\partial A}{\partial y} dy = y dx + x dy$ and $|\Delta x| \leq 0.1, |\Delta y| \leq 0.1$. We use $dx = 0.1, dy = 0.1$ with $x = 21, y = 50$; then the maximum error in the area is about $dA = 21(0.1) + 50(0.1) = 7.1 \text{ cm}^2$.